I will talk about optimal maps between surfaces, starting with works of Ancient Greeks (mainly Ptolemy) on maps used in geography , passing through the works of Euler, Lagrange and Lambert on the same subject, and ending with modern works on best Lipschitz maps between surfaces that are used in Teichmüller theory.